

Conic Equations

UVU Math Lab

Colin Brinkerhoff Method

Parabola:

$$\text{Vertex: } (h, k) \quad p = \frac{1}{4a} \quad a = \frac{1}{4p}$$

Case 1:

$$y = a(x - h)^2 + k$$

Axis of symmetry: vertical, $x = h$
Focus: $(h, k + p)$
Directrix: $y = k - p$

Case 2:

$$x = a(y - k)^2 + h$$

Axis of symmetry: vertical, $y = k$
Focus: $(h + p, k)$
Directrix: $x = h - p$

Ellipse:

$$\frac{(x-h)^2}{a^2} + \frac{(y-k)^2}{b^2} = 1 \quad \text{Center } (h, k)$$

Case 1:

$$a > b$$
$$a^2 = b^2 + c^2$$

Major axis: horizontal, $y = k$
Major vertices: $(h \pm a, k)$
Foci: $(h \pm c, k)$

Case 2:

$$b > a$$
$$b^2 = a^2 + c^2$$

Major axis: vertical: $x = h$
Major vertices: $(h, k \pm b)$
Foci: $(h, k \pm c)$

Hyperbola:

$$\text{Center: } (h, k) \quad c^2 = a^2 + b^2 \quad \text{Asymptotes: } y = \pm \frac{b}{a}(x - h) + k$$

Case 1:

$$\frac{(x - h)^2}{a^2} - \frac{(y - k)^2}{b^2} = 1$$

Major axis: horizontal, $y = k$
Major vertices: $(h \pm a, k)$
Foci: $(h \pm c, k)$

Case 2:

$$-\frac{(x - h)^2}{a^2} + \frac{(y - k)^2}{b^2} = 1$$

Major axis: vertical, $x = h$
Major vertices: $(h, k \pm b)$
Foci: $(h, k \pm c)$